

#1611960

Topic: Maths

Sum of the  $1 + 2.3 + 3.5 + 4.7 + \dots$  up to 11 terms is

- A 942
- B 892
- C 946
- D 960

Hint

 $1.1 + 2.3 + 3.5 + 4.7 + \dots$  up to 11

$$\begin{aligned}
 &= \sum_{r=1}^{11} r(2r-1) \\
 &= 2 \sum_{r=1}^{11} r^2 - \sum_{r=1}^{11} r \\
 &= \frac{2 \cdot (11)(12)(23)}{6} - \frac{11(12)}{2} \\
 &= 44(23) - 11(6) \\
 &= 946
 \end{aligned}$$

#1611974

Topic: Maths

If  $\Rightarrow p(q \vee r)$  is false then truth value of  $p, q, r$  is respectively.

- A TTT
- B FFF
- C FTT
- D TFF

Hint

$$p \rightarrow (q \vee r)$$

$$\sim p \vee (q \vee r)$$

$$(A) \sim (T) \vee (T) \vee (T \vee T)$$

$$F \vee (T) = T$$

$$(B) \sim (F) \vee (F) \vee (F \vee F)$$

$$T \vee (F \vee F)$$

$$= T \vee F = T$$

$$(C) \sim (T) \vee (T \vee F)$$

$$F \vee T = T$$

$$(D) \sim (T) \vee (F \vee F)$$

$$F \vee (F \vee F) = F$$

#1611988

Topic: Maths

If the ratio of coefficient of the three consecutive terms in binomial expansion of  $(1+x)^n$  is 2:15:70.

Then the average of these coefficient is

- A 227
- B 232
- C 964
- D 804

**Hint**

$${}^nC_r : {}^nC_{r+1} : {}^nC_{r+2} = 2 : 15 : 70$$

$$\frac{{}^nC_r}{{}^nC_{r+1}} = \frac{2}{15} = \frac{{}^nC_{r+1}}{{}^nC_{r+2}} = \frac{15}{70}; \frac{{}^nC_r}{{}^nC_{r+2}} = \frac{2}{70}$$

$$\frac{(r+1)}{n-r} = \frac{2}{15} \quad \frac{(r+2)}{n-r-1} = \frac{3}{14}$$

$$15r + 15 = 2n - 2r \quad 14r + 28 = 3n - 3r - 3$$

$$17r = 2n - 15 \quad 17r = 3n - 31$$

$$\therefore n = 16; r = 1$$

$$\text{Average} = \frac{{}^nC_r + {}^nC_{r+1} + {}^nC_{r+2}}{3}$$

$$\frac{{}^{16}C_1 + {}^{16}C_2 + {}^{16}C_3}{3} = \frac{16 + 120 + 560}{3}$$

$$= 232g$$

**#1611996****Topic:** MathsIf  $\int e^{\sec x} (\sec x \tan x f(x) + \sec x \tan x + \tan^2 x) dx = e^{\sec x} f(x) + c$ . Then  $f(x)$  is

- A  $\sec x + x \tan x + \frac{1}{2}$
- B  $x \sec x + x \tan x + \frac{1}{2}$
- C  $x \sec x + x^2 \tan x + \frac{1}{2}$
- D  $\sec x + \tan x + \frac{1}{2}$

**Hint**

$$\int e^{\sec x} (\sec x \tan x f(x) + \sec x \tan x + \sec^2 x) dx = e^{\sec x} f(x)$$

Differentiate both side

$$\int e^{\sec x} (\sec x \tan x f(x) + \sec x \tan x + \sec^2 x) dx = e^{\sec x} f'(x) + e^{\sec x} \tan x f(x)$$

$$\therefore \sec x \tan x + \sec^2 x = f'(x)$$

$$\therefore f(x) = \sec x + \tan x + d$$

**#1612004****Topic:** Maths

The domain of the function

$$f(x) = \frac{1}{x^2 - 4} + \ln(x^3 - x)$$

- A  $[-1, 0) \cup (1, \infty)$
- B  $(-1, \frac{1}{2}) \cup (1, 2) \cup (2, \infty)$
- C  $(-1, 0) \cup (1, 2) \cup (2, \infty)$
- D  $(-\infty, 0) \cup (1, 2) \cup (2, \infty)$

**Hint**

$$f(x) = \frac{1}{x^2 - 4} + \ln(x^3 - x)$$

For domain  $x^2 - 4 \neq 0$ 

$$\therefore x \in \mathbb{R} - 2, 2$$

$$\& x^3 - x > 0$$

$$x(x-1)(x+1) > 0$$

$$\begin{array}{c} - + - + \\ \hline -1, 0, 1 \end{array}$$

$$\therefore x \in (-1, 0) \cup (1, \infty)$$

$$\therefore \text{Domain} : \in (-1, 0) \cup (1, 2) \cup (2, \infty)$$

#1612006

Topic: Maths

The area enclosed by the region  $\frac{y^2}{2} \leq x \leq y + 4$  is

A 16

B 8

 C 18

D 12

Hint

$$\frac{y^2}{2} \leq x \leq y + 4$$

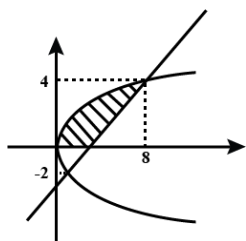
$$y^2 \leq 2x \text{ and } x - y - 4 \leq 0$$

$$\int_{-2}^4 (x_{\text{Right}} - x_{\text{Left}}) dy$$

$$\int_{-2}^4 \left( (y+4) - \frac{y^2}{2} \right) dy$$

$$\left( \frac{y^2}{2} + 4y - \frac{y^3}{6} \right) \Big|_{-2}^4$$

$$= 18$$



#1612038

Topic: Maths

Let  $A = \begin{bmatrix} 0 & 2y & 1 \\ 2x & y & -1 \\ 2x & -y & 1 \end{bmatrix}$  then number of possible matrices that  $A^{-1} = 3I_3$  is

A 3

B 8

C 6

 D 4

**Hint**If  $A^{-1}A = 3I$ , then  $AA^{-1} = 3I$ 

$$\begin{aligned}
 & \begin{bmatrix} 0 & 2y & 1 & 0 & 2x & 2x \\ 2x & y & -1 & 2y & y & -y \\ 2x & -y & +1 & 1 & -1 & 1 \end{bmatrix} \\
 & \begin{bmatrix} (4y^2 + 1) & (2y^2 - 1) & (2y^2 - 1) \\ (2y^2 - 1) & (4x^2 + y^2 + 1) & (4x^2 - y^2 - 1) \\ (-2y^2 + 1) & (4x^2 - y^2 - 1) & (4x^2 + y^2 + 1) \end{bmatrix} \\
 & \begin{bmatrix} 3 & 0 & 0 \\ 0 & 3 & 0 \\ 0 & 0 & 3 \end{bmatrix}
 \end{aligned}$$

$$\therefore 4y^2 + 1 = 3 \therefore y^2 = \frac{1}{2}$$

$$4x^2 + y^2 + 1 = 3$$

$$4x^2 + \frac{1}{2} + 1 = 3$$

$$\therefore 4x^2 = 3 - \frac{3}{2}$$

$$4x^2 = \frac{3}{2} \therefore x^2 = \frac{3}{8}$$

$$(x, y) = \left( \pm \sqrt{\frac{3}{8}}, \pm \frac{1}{\sqrt{2}} \right)$$

(4 such matrices)

#1612041

Topic: Maths

The point lying on common tangent to the circle  $x^2 + y^2 = 4$  and  $x^2 + y^2 + 6x + 8y - 24 = 0$  is

- A (6, -2)
- B (4, -2)
- C (4, 6)
- D (2, 4)

**Hint**Circle  $x^2 + y^2 = 4$  & $x^2 + y^2 + 6x + 8y - 24 = 0$  touches internally $\therefore$  Common tangent will be  $S_1 - S_2 = 0$ 

$$6x + 8y = 20$$

$$3x + 4y - 10 = 0$$

Hence point (6, -2) lies on above line.

#1612051

Topic: Maths

If complex number

$$\omega = \frac{5 + 3z}{5(1 - z)} \text{ and } |z| < 1 \text{ then}$$

- A  $5 \operatorname{Im}(\omega) < 1$
- B  $5 \operatorname{Im}(\omega) > 4$
- C  $5 \operatorname{Re}(\omega) > 1$
- D  $5 \operatorname{Re}(\omega) > 1$

Hint

$$\omega = \frac{5+3z}{5-5z}$$

$$5\omega - 5\omega z = 5 + 3z$$

$$(5\omega + 3)z = 5\omega - 5$$

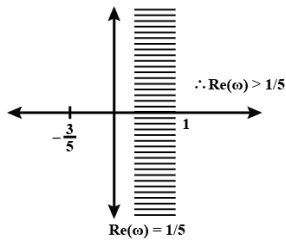
$$z = \frac{5\omega - 5}{5\omega + 3}$$

$$|z| < 1$$

$$\therefore \left| \frac{5\omega - 5}{5\omega + 3} \right| < 1$$

$$|5\omega - 5| < |5\omega + 3|$$

$$|\omega - 1| < \left| \omega + \frac{3}{5} \right|$$



#1612072

Topic: Maths

Let  $\alpha$  and  $\beta$  are the roots of  $(m^2 + 1)x^2 - 3x + (m + 1)^2 = 0$ . If sum of roots is maximum then  $|\theta^3 - \beta^3|$

- A**  $8\sqrt{5}$
- B**  $8\sqrt{3}$
- C**  $10\sqrt{5}$
- D**  $4\sqrt{3}$

Hint

$$(m^2 + 1) - 3x + (m + 1)^2$$

$$\alpha + \beta = \frac{3}{m^2 + 1}$$

$$\alpha\beta = \frac{(m + 1)^2}{m^2 + 1}$$

$$\therefore (\alpha + \beta) = \text{is maximum} \therefore m^2 + 1 \text{ is min}$$

$$\therefore m = 0$$

$$\alpha + \beta = 3, \alpha\beta = 1$$

$$|\theta^3 - \beta^3| = |(\alpha - \beta)(\alpha^2 + \beta^2 + \alpha\beta)|$$

$$= \left| \sqrt{(\alpha + \beta)^2 - 4\alpha\beta} \right|$$

$$|(\alpha + \beta)^2 - \alpha\beta|$$

$$-\sqrt{5} \cdot 8 = 8\sqrt{5}$$

#1612083

Topic: Maths

If a line makes an angle  $\frac{\pi}{3}$  with x-axis,  $\frac{\pi}{4}$  with y-axis then angle made by line with z-axis is

- A**  $\frac{2\pi}{3}$
- B**  $\frac{5\pi}{12}$
- C**  $\frac{3\pi}{4}$
- D**  $\frac{\pi}{12}$

Hint

$$\alpha = \frac{\pi}{3}; \beta = \frac{\pi}{4}$$

$$\therefore \cos^2 \alpha + \cos^2 \beta + \cos^2 \gamma = 1$$

$$\frac{1}{2} + \frac{1}{2} + \cos^2 \gamma = 1$$

$$\cos^2 \gamma = \frac{1}{4}$$

$$\therefore \cos \gamma = \pm \frac{1}{2}$$

$$\gamma = \frac{2\pi}{3}$$

#1612099

Topic: Maths

If two points B and C at distance of 5 units from each other, lie on the line  $\frac{x+2}{3} = \frac{y-1}{0} = \frac{z}{4}$ . If point A has coordinates (1, -1, 2). Then the area of  $\triangle ABC$  is

- A  $\sqrt{34}$
- B  $2\sqrt{34}$
- C  $\sqrt{41}$
- D  $3\sqrt{34}$

Hint

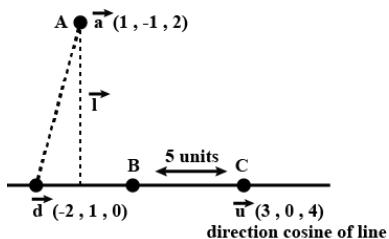
$$|\vec{r}| = |(\vec{a} - \vec{d}) \times \vec{u}|$$

$$|\vec{r}| = \left| (3\vec{i} - 2\vec{j} + 2\vec{k}) \times \left( \frac{3}{5}\vec{i} + \frac{4}{5}\vec{k} \right) \right|$$

$$\left| -\frac{8}{5}\vec{i} + \frac{6}{5}\vec{j} + \frac{6}{5}\vec{k} \right|$$

$$\sqrt{\frac{136}{25}}$$

$$\text{Area of triangle} = \frac{1}{2} \times 5 \times \sqrt{\frac{136}{25}} = \sqrt{34} \text{ units}^2$$



#1612125

Topic: Maths

If  $y(x)$  satisfies the differential equation  $\cos x \frac{dy}{dx} - y \sin x = 6x$  and  $y\left(\frac{\pi}{3}\right) = 0$ . Then value of  $y\left(\frac{\pi}{6}\right)$  is

- A  $\frac{\pi^2}{3\sqrt{2}}$
- B  $\frac{-\pi^2}{3\sqrt{2}}$
- C  $\frac{\pi^2}{2\sqrt{3}}$
- D  $\frac{\pi^2}{4}$

**Hint**

$$\frac{dy}{dx} = y \tan x - 6x \sec x.$$

Linear Diffraction equation in 'y'

$$I. F = e^{\int \tan x dx} = e^{-\ln(\sec x)} = \cos x$$

$$y = (I. F.) = \int Q. (I. F.) dx$$

$$y(\cos x) = \int 6x dx$$

$$y. \cos x = 3x^2 + c$$

$$\therefore y\left(\frac{\pi}{3}\right) = 0$$

$$0 = 3\left(\frac{\pi^2}{9}\right) + c$$

$$\therefore c = \frac{-2\pi^2}{3}$$

$$y \cos x = 3x^2 - \frac{\pi^2}{3}$$

$$\text{when } x = \frac{\pi}{6}$$

$$y \frac{\sqrt{3}}{2} = 3 \cdot \frac{\pi^2}{36} - \frac{\pi^2}{3}$$

$$y \frac{\sqrt{3}}{2} = \frac{-\pi^2}{4}$$

$$y = \frac{-\pi^2}{2\sqrt{3}}$$

#1612137

Topic: Maths

There are two newspaper A & B published in a city, If 25% people read A, 20% people read B & 8% both read. Also 30% of these who read A both not B look into advertisement 40% of these who read B but not A look into advertisement 50 of these who read both A & B look into advertisement then how many % of people into advertisement.

- A 13.9%
- B 13%
- C 13.1%
- D 13.2%

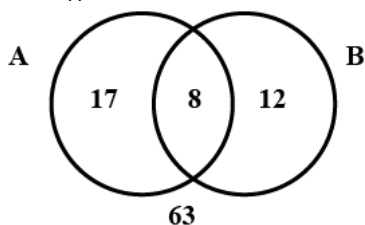
**Hint**

Let total number of persons=100

25 read A

20 read B

8 read A &amp; B

40% of  $\bar{A} \cap B = 4.8$  look into adv.30% of  $\bar{A} \cap B = 4.8$  look into adv.

#1612138

Topic: Maths

There are two towers of  $5m$  &  $10m$ . The line joining their tops makes  $15^\circ$  with ground then find the distance between them.

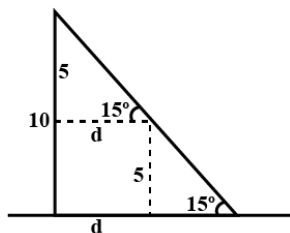
- A  $5(1 - \sqrt{3})$
- B  $10(1 + \sqrt{3})$
- C  $5(2 + \sqrt{3})$

D  $2(2 + \sqrt{3})$

Hint

$$\tan 15^\circ = \frac{5}{d} = 2 - \sqrt{3}$$

$$d = \frac{5}{2 - \sqrt{3}} = 5(2 + \sqrt{3})$$



#1612140

Topic: Maths

If the sum of first 3 terms of an A.P. is 33 and their product is 1155. Then the 11th term of the A.P. is

- A -25
- B 25
- C 36
- D -36

Hint

$$a - d, a, a + d$$

$$\text{Sum} = 3a = 33 \Rightarrow a = 11$$

$$\text{Terms} = 11 - d, 11, 11 + d$$

$$\text{Product} = 11(121 - d^2) = 1155$$

$$121 - d^2 = 105$$

$$d^2 = 16$$

$$d = \pm 4$$

$$\therefore \text{terms } 7, 11, 15 \text{ or } 15, 11, 17$$

$$t_{11} = 7 + 10(4) \quad t_{11} = 15 + 10(-4)$$

$$= 47 \quad = -25$$

#1612141

Topic: Maths

An inverted cone with semi vertex angle  $\theta = \tan^{-1}\left(\frac{1}{2}\right)$  is being filled with water at the rate of  $5\text{cm}^3/\text{min}$ . Then the rate of change of height of water when height of water is

10 cm is

- A  $\frac{2}{3\pi}$  cm/min
- B  $\frac{3}{2\pi}$  cm/min
- C  $\frac{1}{5\pi}$  cm/min
- D  $\frac{2}{5\pi}$  cm/min



Hint

$$\frac{dv}{dt} = 5 \text{ cm}^3/\text{min}$$

$$v = \frac{1}{3} \pi r^2 h$$

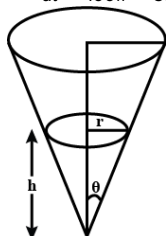
$$\tan \theta = \frac{r}{h} = \frac{1}{2} \Rightarrow 2r = h$$

$$v = \frac{1}{3} \pi \frac{h^3}{4} = \frac{\pi h^3}{12}$$

$$\Rightarrow \frac{dv}{dt} = \frac{\pi}{4} h^2 \frac{dh}{dt}$$

$$5 = \frac{\pi}{4} 10^2 \frac{dh}{dt}$$

$$\Rightarrow \frac{dh}{dt} = \frac{20}{100\pi} = \frac{1}{5\pi} \text{ cm/min}$$



#1612143

Topic: Maths

If points  $A(-8, 5)$  &  $B(6, 5)$  lie on a circle  $C_1$ . The line  $3y = x + 7$  is a diameter of  $C_1$ . Rectangle  $ABCD$  which is inscribed inside the circle is completed. Then the area of this rectangle is

A 60

 B 84

C 42

D 74

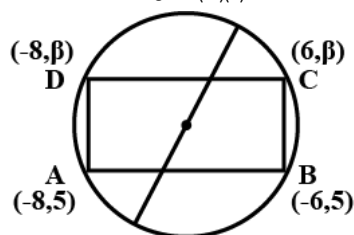
Hint

 $A(-8, 5); B(6, 5)$ 

mid point of  $AC = \left(-1, \frac{\beta + 5}{2}\right)$  lies on  $3y = x + 7$

$$\frac{3}{2}(\beta + 5) = 6 \Rightarrow \beta + 5 = 4 \Rightarrow \beta = -1$$

$$\therefore \text{Area of rectangle} = (14)(6) = 84$$



#1612144

Topic: Maths

Let  $y^2 = 4x$  is a parabola. Then minimum area of a circle touching parabola at  $(1, 2)$  as well as x-axis is

 A  $4\pi(3 - 2\sqrt{2})$ B  $8\pi(3 - 2\sqrt{2})$ C  $8\pi(4 - 2\sqrt{2})$ D  $8\pi(3 - 5\sqrt{2})$

**Hint**

Equation of tangent at (1, 2)

$$2y = 2(x+1) \Rightarrow y = x+1$$

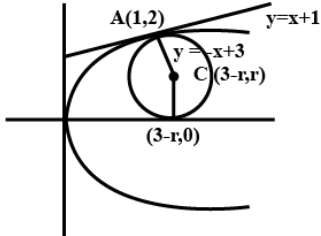
Equation of normal  $y = -x+3$ Let centre be  $C(3-r, r)$ 

$$AC^2 = r^2 \Rightarrow (3-r-1)^2 + (r-2)^2 = r^2$$

$$2(2-r)^2 = r^2 \Rightarrow r^2 - 8r + 8 = 0 \Rightarrow r = 4 \pm 2\sqrt{2}$$

For  $r = 4 + 2\sqrt{2}$ ,  $3-r < 0$ So,  $r = 4 - 2\sqrt{2}$ 

$$\text{Area} = \pi r^2 = 8\pi(3 - 2\sqrt{2})$$



#1612146

Topic: Maths

The mean and median of 10, 22, 26, 29, 34, x, 42, 67, 70, y (in increasing order) are 42 and 35 respectively then the value  $\frac{y}{x}$  is

- A  $\frac{9}{2}$
- B  $\frac{5}{3}$
- C  $\frac{7}{3}$
- D  $\frac{7}{2}$

**Hint**

Median is 35

$$35 = \frac{34+x}{2}$$

$$x = 70 - 34$$

$$= 36$$

$$10\mu = 10 + 22 + 26 + 24 + 29 + 34 + x + 42 + 67 + 70 + y$$

$$420 = 39 + 48 + 70 + 109 + 70 + y$$

$$350 = 87 + 179 + y$$

$$y = 350 - 266$$

$$y = 84$$

$$\frac{y}{x} = \frac{84}{36} = \frac{21}{9} = \frac{7}{3}$$

#1612147

Topic: Maths

If tangent of  $y^2 = x$  at  $(\alpha, \beta)$ , where  $\beta > 0$  is also a tangent of ellipse  $x^2 + 2y^2 = 1$  then value of  $\alpha$  is

- A  $\sqrt{2} - 1$
- B  $\sqrt{2} + 1$
- C  $2\sqrt{2} + 1$
- D  $2\sqrt{2} - 1$

**Hint**

Let required point of contact be  $(\beta^2, \beta)$

Tangent on  $y^2 = x$  is  $T = 0$

$$y \cdot \beta = \frac{1}{2}(x + \beta^2)$$

$$y = \frac{x}{2\beta} + \frac{\beta}{2}$$

Equation of ellipse is  $x^2 + \frac{y^2}{1/2} = 1$

Condition for tangency  $c^2 = a^2 m^2 + b^2$

$$\frac{\beta^2}{4} = 1 \left( \frac{1}{4\beta^2} \right) + \frac{1}{2}$$

$$\Rightarrow \beta^4 = 2\beta^2 + 1 \Rightarrow (\beta^2 - 1)^2 = 2$$

$$\Rightarrow \beta^2 = \sqrt{2} + 1$$

$$\therefore \alpha = \sqrt{2} + 1$$

**#1612148****Topic:** Maths

$$\int_0^1 x \cot^{-1}(1 - x^2 + x^4) dx =$$

A  $\frac{\pi}{2} - \log 2$

B  $\frac{\pi}{2} + \log \sqrt{2}$

C  $\frac{\pi}{4} - \log 2$

D  $\frac{\pi}{4} - \log \sqrt{2}$

**Hint**

$$\int_0^1 x \tan^{-1} \left( \frac{1}{1 - x^2 + x^4} \right) dx$$

$$\Rightarrow \text{put } x^2 = t$$

$$= \frac{1}{2} \int_0^1 \tan^{-1} \left( \frac{1}{1 - t + t^2} \right) dt$$

$$= \frac{1}{2} \int_0^1 \tan^{-1} \left( \frac{t + (1 - t)}{1 - t(1 - t)} \right) dt$$

$$= \frac{1}{2} \int_0^1 (\tan^{-1} t + \tan^{-1}(1 - t)) dt$$

$$= \frac{1}{2} \int_0^1 (\tan^{-1}(1 - t)) dt + \frac{1}{2} \int_0^1 (\tan^{-1}(1 - t)) dt$$

$$\int_0^1 (\tan^{-1}(1 - t)) dt = \int_0^1 (\tan^{-1}(t)) dt$$

$$\text{Put } \tan^{-1} t = k$$

$$\int \frac{\pi}{4} k \sec^2 k dk$$

$$= \frac{\pi}{4} - \frac{1}{2} \log 2 \text{ (using by parts)}$$

**#1612150****Topic:** Maths

The value of  $\sin 10^\circ \cdot \sin 30^\circ \cdot \sin 50^\circ \cdot \sin 70^\circ$  is

A  $\frac{1}{36}$

B  $\frac{1}{32}$

C  $\frac{1}{18}$

D  $\frac{1}{16}$

Hint

$$(\sin 30^\circ)(\sin 10^\circ)(\sin(60^\circ - 10^\circ))(\sin(60^\circ + 10^\circ)) = \frac{1}{2} \left( \frac{1}{4} \sin 30^\circ \right) = \frac{1}{16}$$

#1612152

Topic: Maths

$$\text{If } f(x) = \begin{cases} a|\pi - x| + 1 & x \leq 5 \\ b|x - \pi| + 3 & x > 5 \end{cases}$$

is continuous  $\forall x \in \mathbb{R}$ . Then value of  $a - b$  is

A  $\frac{1}{5 - \pi}$

B  $\frac{2}{5 - \pi}$

C  $\frac{2}{5 + \pi}$

D  $\frac{1}{5 + \pi}$

Hint

We have to check only at  $x = 5$ 

$$f(5) = a|\pi - 5| + 1 = a(5 - \pi) + 1 = f(5^-)$$

$$f(5^+) = b|5 - \pi| + 3 = b(5 - \pi) + 3$$

$$f(5) = f(5^-) = f(5^+)$$

$$a(5 - \pi) + 1 = b(5 - \pi) + 3$$

$$(a - b)(5 - \pi) = 2$$

$$\therefore a - b = \frac{2}{5 - \pi}$$

#1612153

Topic: Maths

If the lines  $x + (a - 1)y = 1$  and  $2x + a^2y = 1$  where  $a \in \mathbb{R} - \{0, 1\}$  are perpendicular to each other. Then distance of their points of intersection from the origin is

A  $\frac{5}{2}$

B  $\frac{2}{\sqrt{5}}$

C  $\frac{\sqrt{5}}{2}$

D  $\sqrt{\frac{2}{5}}$

Hint

$$x + (a - 1)y = 1$$

$$2x + a^2y = 1$$

lines are perpendicular

$$\therefore 1 \times 2 + a^2(a - 1) = 0$$

$$\Rightarrow a^3 + a^2 - 2a^2 - 2a + 2a + 2 = 0$$

$$\Rightarrow a^2(a + 1) - 2a(a + 1) + 2(a + 1) = 0$$

$$\Rightarrow (a + 1)(a^2 - 2a + 2) = 0$$

$$\Rightarrow a = -1$$

$$\therefore \text{lines are } x - 2y = 1$$

$$2x + y = 1$$

$$\Rightarrow -x - 3y = 0 \Rightarrow x = -3y$$

$$\therefore -5y = 1 \Rightarrow y = -\frac{1}{5}, x = \frac{3}{5}$$

$$\text{required distance} = \sqrt{\frac{9}{25} + \frac{1}{25}} = \sqrt{\frac{10}{25}} = \sqrt{\frac{2}{5}}$$

#1612156

Topic: Maths

If some balls are arranged in the form of an equilateral triangle with  $n$  rows such that  $r^{\text{th}}$  row of balls has  $r$  balls in it. If 99 more balls are added to existing one and the balls can now form a square with  $(n-2)$  balls in each row. Then the number of balls that formed the equilateral triangle.

- A** 190  
**B** 290  
**C** 100  
**D** 140

Hint

$$\frac{n(n+1)}{2} + 99 = (n-2)^2 \Rightarrow n^2 - 9n - 190 = 0 \Rightarrow n = 19 \Rightarrow \text{number of balls} = \frac{19 \cdot 20}{2} = 190$$

#1612159

Topic: Maths

Let  $f(2) = 6$  the value of  $\lim_{x \rightarrow 2} \int_6^{f(x)} \frac{2tdt}{x-2}$

- A**  $12f'(2)$   
**B**  $24f'(2)$   
**C**  $8f'(2)$   
**D**  $10f'(2)$

Hint

$$f(2) = 6$$

$$\lim_{x \rightarrow 2} \int_6^{f(x)} \frac{2tdt}{x-2}$$

$$\lim_{x \rightarrow 2} \frac{\int_6^{f(x)} 2tdt}{x-2} \quad (\text{using L.H. Rule})$$

$$= \lim_{x \rightarrow 2} \frac{2f(x) \cdot f'(x)}{1}$$

$$= 12f'(2)$$

#1612164

Topic: Maths

If  $f(x) = (x) - \left[ \frac{x}{4} \right]$  then

- A**  $\lim_{x \rightarrow 4^+} f(x)$  and  $\lim_{x \rightarrow 4^-} f(x)$  both does not exit  
**B** function  $f(x)$  is continuous at  $x = 4$   
**C**  $\lim_{x \rightarrow 4^+} f(x)$  and  $\lim_{x \rightarrow 4^-} f(x)$  both exit but are not equal  
**D**  $\lim_{x \rightarrow 4^+} f(x)$  and  $\lim_{x \rightarrow 4^-} f(x)$  does not exit

Hint

$$f(x) = [x] - \left[ \frac{x}{4} \right]$$

$$\lim_{h \rightarrow 0^+} [4+h] - \left[ \frac{4+h}{4} \right]$$

$$4 - 1 = 3$$

$$\lim_{h \rightarrow 0^+} [4-h] - \left[ \frac{4-h}{4} \right]$$

$$3 - 0 = 3$$

$$f(4) = [4] - [1] = 3$$

$f(x)$  continuous at  $x = 4$

#1612165

Topic: Maths

Let the system of linear equations  $2x + 3y - z = 0$ ,  $2x + ky - 3z = 0$  and  $2x - y + z = 0$  have non trivial non trivial solution then  $\frac{x}{y} + \frac{y}{z} + \frac{z}{x} + k$  will be

A 2

**B** 3

C 1

D -4

Hint

$$\begin{vmatrix} 2 & 3 & -1 \\ 2 & k & -3 \\ 2 & -1 & 1 \end{vmatrix} = 0$$

$$R_2 \rightarrow R_2 - R_1 \text{ and } R_3 \rightarrow R_3 - R_1$$

$$\begin{vmatrix} 2 & 3 & -1 \\ 0 & k-3 & -2 \\ 0 & -4 & 2 \end{vmatrix} = 0$$

$$\Rightarrow k = 7$$

$$\text{Equation 1} \Rightarrow 2\frac{x}{y} + 3 - \frac{z}{y} = 0 \dots\dots(\text{iv})$$

$$\text{Equation 3} \Rightarrow 2\frac{x}{y} - 1 + \frac{z}{y} = 0$$

$$\text{adding these two equation we get } 4\frac{x}{y} + 2 = 0$$

$$\Rightarrow \frac{x}{y} = -\frac{1}{2} \dots\dots(\text{v})$$

$$\text{Putting this value in equation (iv) we get } \frac{z}{y} = 2 \dots\dots(\text{vi})$$

$$\text{Equation (v) divided by equation (vi)} \Rightarrow \frac{x}{z} = -\frac{1}{4}$$

$$\text{So, } \frac{x}{y} + \frac{y}{z} + \frac{z}{x} + k = -\frac{1}{2} + \frac{1}{2} - 4 + 7 = 3$$