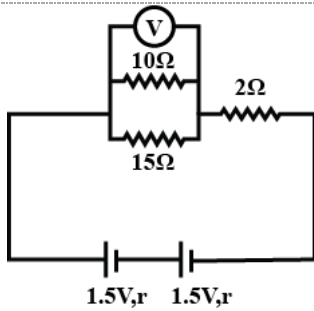


#1612238

Topic: Circuit Instruments



If the reading of the ideal voltmeter shown in the circuit is  $2\text{ V}$  the internal resistance of the two identical cells is

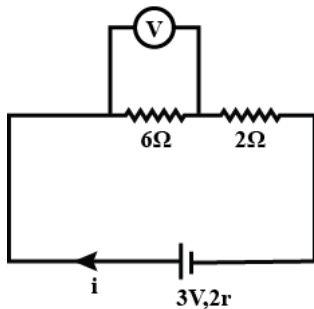
- A  $1\Omega$
- B  $0.5\Omega$**
- C  $1.5\Omega$
- D  $2\Omega$

**Solution**

$$i = \frac{3}{8 + 2r}$$

$$\therefore \text{Reading of voltmeter} = i \times 6 = \frac{3}{8 + 2r} \times 6 = 2$$

$$\Rightarrow 2r + 8 = 9 \Rightarrow r = \frac{1}{2}\Omega$$



#1612240

Topic: Speed of Sound

A stationary source of sound is emitting sound of frequency  $500\text{ Hz}$ . Two observers A and B lying on the same line as the source, observe frequencies  $480\text{ Hz}$  and  $530\text{ Hz}$  respectively. The velocity of A and B respectively are (in  $\text{m/s}$ ), speed of sound =  $300\text{ m/s}$ .

- A 12, 18**
- B 8, 18
- C 18, 8
- D 18, 12

**Solution**

$$f_A = \left( \frac{300 - V_A}{300} \right) \times 500 = 480$$

$$\Rightarrow 15000 - 50V_A = 14400$$

$$\Rightarrow \frac{600}{50} = V_A \Rightarrow V_A = 12\text{ m/s}$$

$$f_B = \left( \frac{300 + V_B}{300} \right) \times 500 = 530$$

$$\Rightarrow V_B + 300 = 318$$

$$V_B = 18\text{ m/s}$$

#1612245

Topic: Acceleration due to Gravity

The height above the surface of earth at which acceleration due to gravity is half the acceleration due to gravity at surface of earth is ( $R = 6.4 \times 10^6 m$ )

- A  $6.4 \times 10^6 m$
- B  $2.6 \times 10^6 m$**
- C  $12.8 \times 10^6 m$
- D  $19.2 \times 10^6 m$

Solution

$$\frac{g}{2} = \frac{Gm}{(R+h)^2}$$

$$g = \frac{Gm}{R^2}$$

$$\frac{1}{2} = \frac{R^2}{(R+h)^2}$$

$$R+h = \sqrt{2}R$$

$$R = 0.41R$$

$$= 0.41 \times 6.4 \times 10^6 m = 2.6 \times 10^6 m$$

#1612250

Topic: Free, Forced and Damped Oscillations

Equation of motion for a particle performing damped harmonic oscillation is given as  $x = e^{-1t} \cos(10\pi t + \phi)$ . The times when amplitude will half of the initial is :

- A 27
- B 4
- C 1
- D 7**

Solution

$$\frac{A_0}{2} = A_0 e^{-0.1t} \Rightarrow e^{-0.1t} = \frac{1}{2} \Rightarrow 0.1t = \ln 2$$

$$t = \frac{\ln 2}{0.1} = 10 \ln 2 = 6.93 \approx 7s$$

#1612253

Topic: Change in Nucleus due to Radioactive decay

A sample containing same number of two nuclei A and B start decaying. The decay constant of A and B are  $10\lambda$  and  $\lambda$ . The time after which  $\frac{N_A}{N_B}$  becomes  $\frac{1}{e}$  is

- A  $\frac{1}{9\lambda}$**
- B  $\frac{1}{18\lambda}$
- C  $\frac{2}{9\lambda}$
- D  $\frac{3}{19\lambda}$

Solution

$$\frac{N_A}{N_B} = \frac{N_0 e^{-10\lambda t}}{N_0 e^{-\lambda t}} = \frac{1}{e}$$

$$\Rightarrow e^{-9\lambda t} = e^{-1}$$

$$\Rightarrow 9\lambda t = 1$$

$$\Rightarrow t = \frac{1}{9\lambda}$$

#1612262

Topic: Drift of electrons

In conducting wire of radius 5 mm, resistivity  $\rho = 1.1 \times 10^{-8} \Omega/m$  and current of 5A is flowing. Drift velocity of free electron is  $1.1 \times 10^{-3} m/s$  find out mobility of free electron.

- A**  $1.57 \text{ m}^2 \text{ volt/sec}$
- B**  $1.25 \text{ m}^2 \text{ volt/sec}$
- C**  $1.2 \text{ m}^2 \text{ volt/sec}$
- D**  $2 \text{ m}^2 \text{ volt/sec}$

**Solution**

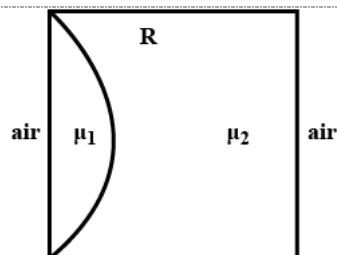
$$V_d = \mu E = \mu \frac{V}{\rho}$$

$$V_d = \frac{\mu}{\rho} \frac{IR}{A\rho} = \frac{\mu}{A} \frac{I_p}{\rho}$$

$$\mu = \frac{V_d A}{I_p} = \frac{1.1 \times 10^{-3} \times \lambda \times 25 \times 10^{-6}}{5 \times 1.1 \times 10^{-8}}$$

$$\mu = 1.57 \text{ m}^2 \text{ volt/sec.}$$

#1612277

**Topic:** Combination of Lenses and Mirrors

Find out equivalent focal length of given lens combination

- A**  $\left( \frac{R}{\mu_1 - \mu_2} \right)$
- B**  $\left( \frac{2R}{\mu_1 - \mu_2} \right)$
- C**  $\left( \frac{4R}{\mu_1 - \mu_2} \right)$
- D**  $\left( \frac{R}{\mu_1 + \mu_2} \right)$

**Solution**

$$\frac{1}{f_1} = (\mu_1 - 1) \left( \frac{1}{\infty} - \frac{1}{-R} \right) = \frac{\mu_1 - 1}{R}$$

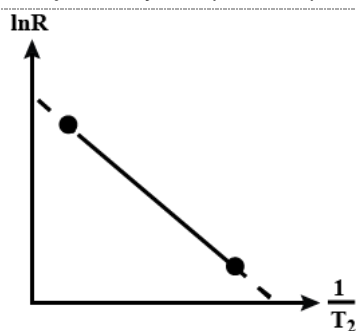
$$\frac{1}{f_2} = (\mu_2 - 1) \left( \frac{1}{-R} - \frac{1}{\infty} \right) = \frac{\mu_2 - 1}{-R}$$

$$\frac{1}{f_{eq}} = \left( \frac{\mu_1 - 1}{R} \right) - \left( \frac{\mu_2 - 1}{R} \right)$$

$$f_{eq} = \left( \frac{R}{\mu_1 - \mu_2} \right)$$

#1612288

**Topic:** Graphs in Kinematics



The graph shows the variation of  $\ln R$  v/s  $\frac{1}{T}$ , where R is resistance and T is temperature. Then find R as function of T.

- A**  $R = R_0 e^{-T_0^2 / T^2}$
- B**  $R = R_0 e^{-T^2 / T_0^2}$
- C**  $R = R_0 e^{T^3 / T_0}$
- D**  $R = R_0 e^{-T^3 / T_0^3}$

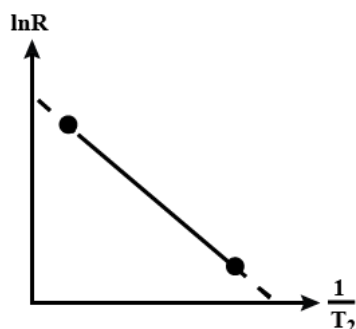
**Solution**

$$y = mx + c$$

$$\ln R = -m \frac{1}{T^2} + c$$

$$R = e^{-\frac{m}{T^2} \times e^c}$$

$$R = R_0 e^{-\frac{T_0^2}{T^2}}$$



#1612308

**Topic:** Basics of Moment of Inertia

Two uniform circular rough disc of moment of inertia  $I_1$  and  $\frac{I_1}{2}$  are rotating with angular velocity  $\omega_1$  and  $\frac{\omega_1}{2}$  respectively in same direction. Now one disc is placed the other disc co-axially. The change in kinetic energy of the system is :

- A**  $-\frac{1}{24} I_1 \omega_1^2$
- B**  $\frac{1}{24} I_1 \omega_1^2$
- C**  $\frac{1}{12} I_1 \omega_1^2$
- D**  $-\frac{1}{12} I_1 \omega_1^2$

**Solution**

$$\vec{L}_i = \vec{L}_f$$

$$I_1 \omega_1 + \frac{I_1 \omega_1}{2} = I_1 \omega_f + \frac{I_1 \omega_f}{2}$$

$$\frac{5I_1 \omega_1}{4} = \frac{3}{2} I_1 \omega_f \quad \omega_f = \frac{5}{6} \omega_1$$

$$\Delta K.E. = \left( \frac{1}{2} I_1 \omega_f^2 + \frac{1}{2} \frac{I_1}{2} \omega_f^2 \right) - \left( \frac{1}{2} I_1 \omega_1^2 + \frac{1}{2} \frac{I_1}{2} \left( \frac{\omega_1}{2} \right)^2 \right)$$

$$= \frac{1}{2} \cdot \frac{3}{2} I_1 \frac{25}{36} \omega_1^2 - \frac{1}{2} \cdot \frac{9}{8} I_1 \omega_1^2$$

$$= \frac{75 I_1 \omega_1^2}{144} - \frac{9}{8} I_1 \omega_1^2$$

$$= \frac{75 - 81}{144} I_1 \omega_1^2$$

$$\Delta K.E. = -\frac{1}{24} I_1 \omega_1^2$$

#1612332

Topic: Lorentz Force

An electron, a proton and a  $He^+$  ion projected into a magnetic field with same kinetic energy, with velocities being perpendicular to the magnetic field. The order of the radii of circles traced by them is:

A  $r_p > r_{He^+} > r_e$

☒ B  $r_{He^+} > r_p > r_e$

C  $r_p = r_{He^+} > r_e$

D None of these

Solution

radius of circle is given by

$$r = \frac{mv}{qB} = \frac{p}{qB} = \frac{\sqrt{2mk}}{qB} = \frac{\sqrt{2m}}{qB} \sqrt{k}$$

where K is kinetic energy

For proton

$$r_p = \frac{\sqrt{2m_p}}{eB} \sqrt{k}$$

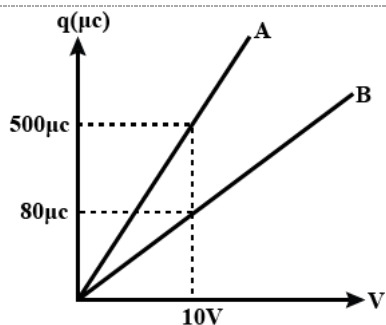
$$\text{for electron } r_e = \frac{\sqrt{2m_e}}{eB} \sqrt{k}$$

$$\text{for } He^+ \quad r_{He^+} = \frac{\sqrt{2 \times 4m_p}}{eB} \sqrt{k} = \frac{2\sqrt{2m_p}}{eB} \sqrt{k}$$

Clearly  $r_{He^+} > r_p > r_e$

#1612334

Topic: Equivalent Capacitance in series-parallel



Plot A & B represent variation of charge with potential difference across the combination (series and parallel) of two capacitors. Then find the value of capacitance of capacitors.

A  $20\text{ }\mu\text{F}, 30\text{ }\mu\text{F}$

☒ B  $10\text{ }\mu\text{F}, 40\text{ }\mu\text{F}$

C  $10\text{ }\mu\text{F}, 15\text{ }\mu\text{F}$

D  $25\mu F, 25\mu F$ **Solution**

For parallel combination -

$$q = 10(C_1 + C_2)$$

$$q_1 = 500\mu C$$

$$500 = 10(C_1 + C_2)$$

$$C_1 + C_2 = 50\mu F \dots (i)$$

For series combination

$$q_2 = 10 \frac{C_1 C_2}{C_1 + C_2}$$

$$80 = 10 \frac{C_1 C_2}{50} \text{ From equation ... (i)}$$

$$C_1 C_2 = 400 \dots (ii)$$

From equation (i) and (ii)

$$C_1 = 10\mu F \quad C_2 = 40\mu F$$

#1612335

Topic: Transistor

Power gain for  $N-P-N$  transistor is  $10^6$ , input resistance  $100\Omega$  and output resistance  $1000\Omega$ . find out current gain.

A 100

B 150

C 200

D 50

**Solution**

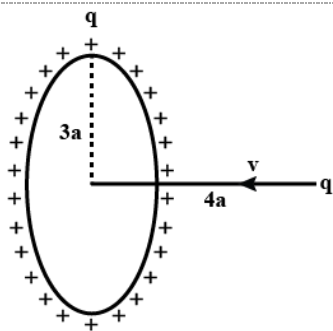
$$\text{Power gain} = (\text{Current gain})^2 \left( \frac{R_{out}}{R_{in}} \right)$$

$$10^6 = \beta^2 \times \frac{10^4}{100}$$

$$\beta = 100$$

#1612336

Topic: Basics of Projectile Motion



A Circular ring of radius  $3a$  is uniformly charged with charge  $q$  is kept in  $x-y$  plane with center at origin. A particle of charge  $q$  and mass  $m$  is projected from  $x = 4a$  towards origin. Find the minimum speed of projection such that it reaches origin.

A  $\sqrt{\frac{q^2}{15\pi\epsilon_0 ma}}$

B  $\sqrt{\frac{q^2}{30\pi\epsilon_0 ma}}$

C  $\sqrt{\frac{q^2}{10\pi\epsilon_0 ma}}$

$$D \quad \sqrt{\frac{q^2}{20\pi\epsilon_0 ma}}$$

**Solution**

$$W_{\text{ext}} + W_{i.n.c.} = \Delta KE + \Delta U$$

$$0 = \left(0 - \frac{1}{2}mv^2\right) + q\left(\frac{kq}{3a} - \frac{kq}{5a}\right)$$

$$\frac{1}{2}mv^2 = \frac{2kq^2}{15a}$$

$$v = \sqrt{\frac{4Kq^2}{15ma}} = \sqrt{\frac{q^2}{15\pi\epsilon_0 ma}}$$

#1612337

**Topic:** Isobaric, Isochoric, Isothermal Processes

An Ideal gas undergoes an isobaric process. If its heat capacity is  $C_v$  at constant volume and number of mole  $n$ , then the ratio of work done by gas to heat given to gas when temperature of gas changes by  $\Delta T$  is:

$$A \quad \left(\frac{nR}{C_v + R}\right)$$

$$B \quad \left(\frac{R}{C_v + R}\right)$$

$$C \quad \left(\frac{nR}{C_v - R}\right)$$

$$D \quad \left(\frac{R}{C_v - R}\right)$$

**Solution**

$$\frac{f}{2}R = \frac{C_v}{n}$$

$$W = nR\Delta T$$

$$\Delta Q = \left(\frac{f}{2} + 1\right)nR\Delta T$$

$$\frac{W}{\Delta Q} = \left(\frac{2}{f+2}\right) = \frac{2}{\frac{2C_v}{nR} + 2} = \left(\frac{nR}{C_v + R}\right)$$

#1612338

**Topic:** Basics of Moment of Inertia

Surface mass density of a disc of mass  $m$  and radius  $R$  is  $\sigma = Kr^2$ , then its moment of inertia w.r.t. axis of rotation passing through centre and perpendicular to the plane of disc

$$A \quad I = \frac{3}{2}mR^2$$

$$B \quad I = \frac{4}{3}mR^2$$

$$C \quad I = \frac{2}{5}mR^2$$

$$D \quad I = \frac{2}{3}mR^2$$

**Solution**

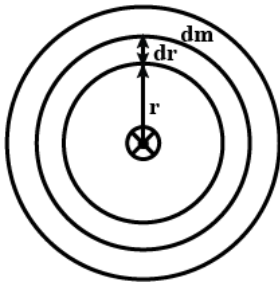
$$dl = dm r^2$$

$$I = \int_0^R K r^2 2\pi r dr. \quad r^2 = k 2\pi \frac{R^6}{6} = \frac{K\pi R^6}{3}$$

$$\int_0^m dm = \int_0^R K r^2 2\pi r dr$$

$$m = 2\pi K \frac{R^4}{4} = \frac{\pi K R^4}{2}$$

$$I = \frac{2}{3} m R^2$$



#1612340

Topic: Amplitude Modulation

A modulating wave of frequency 100 MHz and amplitude 100 V is superimposed on a carrier wave of frequency 300 GHz and amplitude 400 V. the value of modulating index and difference between the maximum frequency and minimum frequency of modulated wave are respectively:

- A  $0.25, 1 \times 10^8 \text{ Hz}$
- B  $4, 2 \times 10^8 \text{ Hz}$
- C  $4, 1 \times 10^8 \text{ Hz}$
- ☒ D  $0.25, 2 \times 10^8 \text{ Hz}$

Solution

$$\text{Modulating index } m = \frac{100}{400} = 0.25$$

$$f_{\max} - f_{\min} = (f_c + f_m) - (f_c - f_m) \\ = 2f_m = 2 \times 10^8 \text{ Hz}$$

#1612344

Topic: Maxwell's Equations

The maximum kinetic energy of electron if wavelength of incident electromagnetic wave is 260 nm and cut-off wavelength is 380 nm given  $hc = 1237 \text{ nm} \cdot \text{eV}$  is

- ☒ A 1.5 eV
- B 6.4 eV
- C 10 eV
- D None of these

Solution

We know

$$KE_{\max} = \frac{hc}{\lambda} - \frac{hc}{\lambda_0} \\ = \frac{1237 \text{ nm} \cdot \text{eV}}{260 \text{ nm}} - \frac{1237 \text{ nm} \cdot \text{eV}}{380 \text{ nm}} \\ = 1.5 \text{ eV}$$

#1612346

Topic: Maxwell's Equations

If  $\vec{E} = E_0 \cos(kz) \cos(\omega t) \hat{j}$  then  $\vec{B}$  for electromagnetic wave is:

- A  $\vec{B} = \frac{E_0}{C} \hat{k}$
- ☒ B  $\vec{B} = \frac{E_0}{C} \sin(kz) \sin(\omega t) \hat{j}$



C  $\vec{B} = \frac{E_0}{C} \sin(kz) \cos(\omega t) \hat{j}$

D  $\vec{B} = \frac{E_0}{C} \cos(kz) \sin(\omega t) \hat{j}$

**Solution**

$$\frac{dE}{dz} = -\frac{dB}{dt}$$

If  $\vec{E} = E_0 \cos(kz) \cos(\omega t) \hat{i}$  then

$$\vec{B} = \frac{E_0}{C} \sin(kz) \sin(\omega t) \hat{j} \text{ will satisfy the equation}$$

**#1612348**

**Topic:** Basics of Projectile Motion

A particle is projected vertically upwards with speed  $v_0$ . The drag force acting on it given by  $f_{\text{drag}} = m\gamma v^2$ . the time when it is at maximum height is:

A  $\frac{1}{\sqrt{g\gamma}} \tan^{-1} \left( \frac{\sqrt{\gamma}}{\sqrt{g}} v_0 \right)$

B  $\sqrt{g\gamma} \tan^{-1} \left( \frac{\sqrt{\gamma}}{\sqrt{g}} v_0 \right)$

C  $\frac{\tan^{-1} \left( \frac{\sqrt{g}}{\sqrt{\gamma}} v_0 \right)}{\sqrt{g\gamma}}$

D  $\frac{1}{\sqrt{g\gamma}} \tan^{-1} \left( \frac{\sqrt{\gamma}}{\sqrt{g}} \frac{1}{v_0} \right)$

**Solution**

$$a = -(g + \gamma v^2)$$

$$\frac{dv}{dt} = -(g + \gamma v^2)$$

$$\int_{v_0}^0 \frac{dv}{g + \gamma v^2} = - \int_0^t dt$$

$$\frac{1}{\gamma} \int_{v_0}^0 \left( \frac{g}{\gamma} + v^2 \right) = - \int_0^t dt$$

$$\frac{1}{\gamma} \left[ \frac{1}{\sqrt{\frac{g}{\gamma}}} \tan^{-1} \left( \sqrt{\frac{g}{\gamma}} v \right) \right]_{v_0}^0 = -t$$

$$\frac{1}{\sqrt{g\gamma}} \tan^{-1} \left( \frac{\sqrt{\gamma}}{\sqrt{g}} v_0 \right) = t$$

**#1612349**

**Topic:** Transformers

In a step-down transform the turn ratio is 1: 2 and output power is 2.2 kW. if output current is 10 A then the value of input voltage and input current:

A 100 V, 20 A

B 110 V, 10 A

C 440 V, 5 A

D 440 V, 20 A

**Solution**

$$P_{\text{out}} = V_0 I_0$$

$$\Rightarrow 2200 = V_0 \times 10 \Rightarrow V_0 = 220 \text{ volt}$$

$$\therefore V - i = 2 \times 220 = 440 \text{ V} (\because N_s/N_p = 1/2 = V_0/V_1)$$

$$\text{Also } 2200 = 440 \times I_i$$

$$\Rightarrow I_i = 5 \text{ A}$$

#1612350

Topic: Viscosity

The depression of mercury in a capillary tube of radius  $R_1$  is observed to be equal to the rise of water in another capillary tube of radius  $R_2$ . If the ratio of surface tension of mercury and water is 7.5, ratio of their density  $\frac{\rho_{Hg}}{\rho_{water}} = 13.6$  and their angle of contact are  $\theta_{Hg} = 135^\circ$  and  $\theta_{water} = 0^\circ$  in the respective tubes then  $R_1/R_2$  is:

A 0.2

**B** 0.4

C 0.7

D 0.8

Solution

$$|h_{Hg}| = |h_{water}|$$

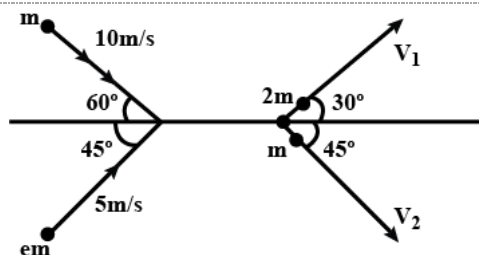
$$\frac{2S_{Hg}\cos\theta_{Hg}}{\rho_{Hg}R_{Hg}g} = \frac{2S_w\cos\theta_w}{\rho_wR_wg}$$

$$\frac{R_{Hg}}{R_w} = \frac{\rho_w}{\rho_{Hg}} \frac{S_{Hg}\cos\theta_{Hg}}{S_w\cos\theta_w} = \frac{1}{13.6} \times 7.5 \times \frac{1}{\sqrt{2}}$$

$$\frac{R_{Hg}}{R_w} = 0.4$$

#1612351

Topic: Elastic Collisions in One-Dimension



Two particle of masses  $m$  and  $2m$  are colliding elastically as given in figure. If  $V_1$  and  $V_2$  speed of particle just after collision then

A  $V_1 = 11.16 \text{ m/s}$ ,  $V_2 = 6.31 \text{ m/s}$ B  $V_1 = 10.16 \text{ m/s}$ ,  $V_2 = 5.31 \text{ m/s}$ C  $V_1 = 9.16 \text{ m/s}$ ,  $V_2 = 6.31 \text{ m/s}$ **D**  $V_1 = 6.31 \text{ m/s}$ ,  $V_2 = 11.16 \text{ m/s}$ 

Solution

Using momentum conservation

In x direction

$$m \times 10 \cos 60^\circ + 2m \frac{5}{\sqrt{2}} = \frac{mv_2}{\sqrt{2}} + 2mv_1 \frac{\sqrt{3}}{2}$$

$$5\sqrt{2} + 10 = v_2 + \sqrt{6}V_1 \dots\dots (A)$$

In Y-direction

$$2m \frac{5}{\sqrt{2}} - m \frac{10\sqrt{3}}{2} = \frac{2mv_1}{2} - \frac{mv_2}{\sqrt{2}}$$

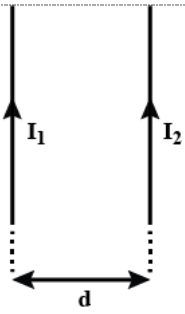
$$10 - 5\sqrt{6} = \sqrt{2}V_1 - V_2 \dots\dots (B)$$

Using A and B

$$V_1 = 6.31 \text{ m/s}, V_2 = 11.16 \text{ m/s}$$

#1612352

Topic: Magnetic field



Two parallel infinite wires separated by distance 'd' carry currents as shown in figure.

The distance from a third infinite wire be kept parallel to wire carrying current  $I_1$ , the wire such that it stays in equilibrium is

- A  $\frac{I_2}{I_2 + I_1}d$  or  $\frac{I_1}{I_1 + I_2}d$
- B**  $\frac{I_2}{I_2 - I_1}d$  or  $\frac{I_1}{I_1 - I_2}d$
- C  $\frac{I_2}{I_1 - I_2}d$  or  $\frac{I_1}{I_1 - I_2}d$
- D  $\frac{2I_2}{I_2 + I_1}d$  or  $\frac{I_1}{I_1 - I_2}d$

#### Solution

For the case when  $I_1 < I_2$

Let the length of the third wire is  $l$  ( $l \rightarrow \infty$ )

For equilibrium  $F_1 = F_2$

$$\Rightarrow \frac{\mu_0 I_1 l}{2\pi x} = \frac{\mu_0 I_2 l}{2\pi(d+x)} \Rightarrow \frac{d+x}{x} = \frac{I_2}{I_1} \Rightarrow \frac{d}{x} = \frac{I_2 - I_1}{I_1} \Rightarrow x = \left( \frac{I_2}{I_2 - I_1} \right) d$$

For the case when  $I_2 < I_1$

$F_1 = F_2$

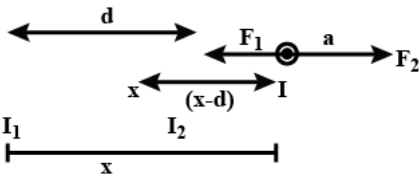
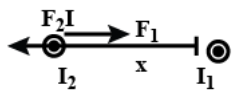
$$\frac{\mu_0 I_1 l}{2\pi x} = \frac{\mu_0 I_2 l}{2\pi(x-d)}$$

$$\Rightarrow \frac{x-d}{x} = \frac{I_2}{I_1}$$

$$\Rightarrow 1 - \frac{d}{x} = \frac{I_2}{I_1} \Rightarrow \frac{I_1 - I_2}{I_1} = \frac{d}{x}$$

$$\Rightarrow x = \left( \frac{I_1}{I_1 - I_2} \right) d$$

$\therefore$  value of  $x$  is  $\frac{I_2}{I_2 - I_1}$  or  $\frac{I_1}{I_1 - I_2}d$



#1612353

Topic: Force and Torque

The coordinates of a particle of mass ' $m$ ' as function of time are given by  $x = x_0 + a_1 \cos(\omega_1 t)$  and  $y = y_0 + a_2 \sin(\omega_2 t)$ . The torque on particle about origin at time  $t = 0$  is:

- A  $(ma_1 \omega_1^2 x_0) \hat{k}$
- B  $(ma_1 \omega_1^2 x_0^2) \hat{k}$
- C**  $(ma_1 \omega_1^2 y_0) \hat{k}$
- D  $(ma_1 \omega_1^2 x_0 y_0) \hat{k}$

#### Solution

$$\vec{r} = (x_0 + a_1 \cos(\omega_1 t))\hat{i} + (y_0 + a_2 \sin(\omega_2 t))\hat{j}$$

$$\vec{v} = -a_1 \omega_1 \sin(\omega_1 t)\hat{i} + a_2 \omega_2 \cos(\omega_2 t)\hat{j}$$

$$\vec{a} = -a_1 \omega_1^2 \cos(\omega_1 t)\hat{i} - a_2 \omega_2^2 \sin(\omega_2 t)\hat{j}$$

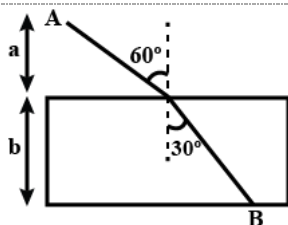
$$\text{at } t = 0, \vec{r} = (x_0 + a_1)\hat{i} + y_0\hat{j}$$

$$\vec{F} = m\vec{a} = -ma_1\omega_1^2\hat{i}$$

$$\vec{r} = \vec{r} \times \vec{F} = (ma_1\omega_1^2 y_0)\hat{k}$$

#1612354

Topic: Prism

For path  $A \rightarrow B$  optical path is

- A**  $2(a + b)$
- B**  $2(a - b)$
- C**  $a + b$
- D**  $a - b$

Solution

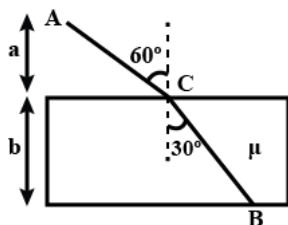
$$AC = \frac{a}{\cos 60^\circ}; CB = \frac{b}{\cos 30^\circ}$$

$$\sin 60^\circ = \mu \sin 30^\circ$$

$$\mu = \sqrt{3}$$

$$\text{optical path} = AC + \mu CB$$

$$= \frac{a}{\cos 60^\circ} + \mu \frac{b}{\cos 30^\circ} = 2a + \sqrt{3} \frac{b}{\frac{\sqrt{3}}{2}} = 2(a + b)$$



#1612355

Topic: Introduction to Kinetic Theory

Rms speed of  $O_2$  molecule is  $200 \text{ m/s}$  at  $T = 300 \text{ K}$  and  $P = 3 \text{ atm}$ . If diameter of molecule is  $0.3 \text{ nm}$  then collision frequency is:

- A**  $2.9 \times 10^7 \text{ s}^{-1}$
- B**  $2.9 \times 10^6 \text{ s}^{-1}$
- C**  $2.9 \times 10^8$
- D**  $2.9 \times 10^5$

Solution

$$\text{Collision frequency} = \sqrt{\frac{8kT}{\pi m}} \cdot \frac{\sqrt{2}\pi d^2 N_A P}{RT}$$

$$= \sqrt{\frac{8}{\pi} \times \frac{25}{3} \times \frac{300}{32}} \cdot \frac{\sqrt{2} \times 9 \times 10^{-29} \times 6.023 \times 10^{23} \times 10^5}{\frac{25}{3} \times 300} = \frac{722.14}{25} \times 10^6$$

$$= 28.8 \times 10^6 = 2.9 \times 10^7 \text{ s}^{-1}$$

#1612356

Topic: Gas Laws

He is kept in a rigid container of volume 67.2 ltr at STP. The heat supplied to the gas to increase its temperature by  $20^{\circ}\text{C}$  is:

A 780 J

☒ B 748 J

C 718 J

D 680 J

Solution

$$Q = nC_V \Delta T = \frac{67.2}{22.4} \cdot \frac{3R}{2} \cdot 20 = 3 \times \frac{3}{2} \times 8.314 \times 20 = 748 \text{ J}$$

#1612357

Topic: Nature of Electromagnetic Waves

Some devices and electromagnetic wave are given in Column -I and Column - II, match the device with electromagnetic wave work:

Column - I	Column - II
(A) Mobile	(P) Microwave
(B) Sonar	(Q) IR
(C) Radar	(R) Radio wave
(D) Optical fiber	(S) Ultra sound

A (A  $\rightarrow$  S); (B  $\rightarrow$  Q), (C  $\rightarrow$  P), (D  $\rightarrow$  R)
☒ B (A  $\rightarrow$  Q); (B  $\rightarrow$  S), (C  $\rightarrow$  P), (D  $\rightarrow$  R)
C (A  $\rightarrow$  Q); (B  $\rightarrow$  S), (C  $\rightarrow$  R), (D  $\rightarrow$  P)D (A  $\rightarrow$  S); (B  $\rightarrow$  Q), (C  $\rightarrow$  R), (D  $\rightarrow$  P)

Solution

1) Mobile – IR,

IR wireless is the use of wireless technology in devices or systems that convey data through infrared (IR) radiation. Infrared is electromagnetic energy at a wavelength or wavelengths somewhat longer than those of red light. The Infrared feature or IR LED as is popularly known, smartphones can now be used as a remote controller for TVs, set top boxes, AC etc

2) SONAR – Ultrasound

The ultrasonic sensor uses sonar to determine the distance to an object.

3) Radar – Microwave

Microwave Radar Sensor module has been designed as an alternative to the common PIR motion sensors widely used in burglar alarms and security lights. Like the PIR (<https://robu.in/product-category/sensors/ir-and-pir-sensors/>) sensor this sensor also detects only movements within its detection range.

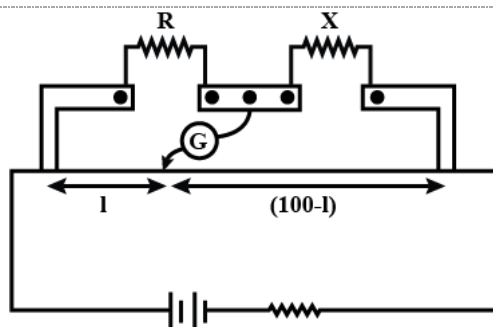
4) Optical Fiber – Radiowaves

Radio over fiber (RoF) or RF over fiber (RfOF) refers to a technology whereby light is modulated by a radio frequency signal and transmitted over an optical fiber ([https://en.wikipedia.org/wiki/Optical\\_fiber](https://en.wikipedia.org/wiki/Optical_fiber)) link. Main technical advantages of using fiber optical links are lower transmission losses and reduced sensitivity to noise and electromagnetic interference compared to all-electrical signal transmission.

(A  $\rightarrow$  Q); (B  $\rightarrow$  S), (C  $\rightarrow$  P), (D  $\rightarrow$  R)

#1612358

Topic: Potentiometer



Which of the above is inconsistent for the given meter bridge:

S.N	R	$\rho$
1.	$1000\Omega$	60 cm
2.	$100\Omega$	13 cm
3.	$10\Omega$	1.5 cm
4.	$1\Omega$	1 cm

A 1

B 2

C 3

**D** 4

**Solution**

$$1) X = \frac{R(100 - l)}{\rho}$$

$$= \frac{1000(100 - 60)}{60}$$

$$= \frac{40,000}{60}$$

$$666.66\Omega$$

$$2) X = \frac{R(100 - l)}{\rho}$$

$$= \frac{100(100 - 13)}{13}$$

$$= \frac{8700}{13}$$

$$= 669.23\Omega$$

$$3) X = \frac{R(100 - l)}{\rho}$$

$$= \frac{10(100 - 15)}{15}$$

$$= \frac{850}{15}$$

$$= 56.66\Omega$$

$$4) X = \frac{R(100 - l)}{\rho}$$

$$= \frac{1(100 - 1)}{1}$$

$$= 99\Omega$$

so answer is 4

#1612360

Topic: Circuit Instruments

Full scale deflection current for a galvanometer is  $10^{-4}A$ . a resistance of  $2 \times 10^6\Omega$  is connected in series. Calculate shunt required to convert into an ammeter of range  $0mA + 10mA$ .

**Solution**

$$R_s = \frac{I_g R_g}{I - I_g}$$
$$\frac{10^{-4} \times (2 \times 10^6)}{0 + 10}$$
$$= \frac{200}{10}$$
$$20\Omega$$

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