

#1612972

Topic: Gas Laws

2 mole ideal He gas and 3 mole ideal H_2 gas at constant volume find out C_v of mixture

- A $\frac{21R}{10}$
- B $\frac{11R}{10}$
- C $\frac{21R}{5}$
- D $\frac{11R}{5}$

Solution

The given mixture of two moles of monoatomic gas mixed with three mole of diatomic gas can be given as

$$C = \frac{n_1 C_{v1} + n_2 C_{v2}}{n_1 + n_2}$$
$$= \frac{2 \times \frac{3}{2}R + 3 \times \frac{5}{2}R}{2 + 3}$$
$$= \frac{3R + 15\frac{R}{2}}{5} = \left(\frac{21R}{10}\right)$$

#1613008

Topic: Atomic Spectra and Spectral Series

He^+ is in n^{th} state. It emits two successive photons of wavelength $103.7nm$ and $30.7nm$, to come to ground state the value of n is:

- A 4
- B 5
- C 6
- D 7

Solution

To find the wavelength in eV we must multiply the given formula by 1240

Thus we get,

$$E_{total} = \left(\frac{1240}{103.7} + \frac{1240}{30.7}\right) eV = 52.34 eV$$

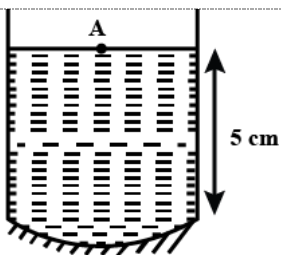
$$52.34 eV = 13.6 \times 4 \left(1 - \frac{1}{n^2}\right)$$

$$n^2 = 25$$

$$n = 5$$

#1613013

Topic: Refraction at Spherical Surfaces



Water is filled in a container upto a height of $5cm$. There is a concave mirror of radius of curvature $40cm$. A person just above the surface observes images of 'A'. The distance of image from water surface is ($\mu_{water} = 1.33$):

- A $8.8cm$

- B 7.8cm
C 6.8cm
D 5.4cm

Solution

Reflection from mirror

$$\frac{1}{v} + \frac{1}{u} = \frac{1}{f}$$

$$\frac{1}{v} + \frac{1}{-5} = \frac{1}{20} \quad \therefore (f = -20cm)$$

$$v = \frac{20}{3} cm$$

Refraction from water surface,

$$\frac{\mu_2}{v} - \frac{\mu_1}{u} = 0$$

$$\frac{1}{v} - \frac{1.33}{\left(\frac{35}{3}\right)} = 0$$

$$v = -\frac{35}{3 \times 1.33} = -8.8cm$$

#1613020

Topic: Specific Heat Capacities

m_1 gram of ice at -10° and m_2 gram of water at $50^\circ C$ are mixed in insulated container. if in equilibrium state we get only water at $0^\circ C$ then latent heat ice is:

- A $\frac{50m_2}{m_1} + 5$
 B $\frac{50m_2}{m_1} - 5$
 C $\frac{50m_2}{m_1} + 50$
 D $\frac{50m_2}{m_1} - 50$

Solution

heat taken by ice = heat given by water

$$m_1 S_{ice}(10) + m_1 = m_2 S_w(50)$$

$$\Rightarrow \frac{m_1}{2} \times 80 + m_1 L_f = m_2 \times 50$$

$$\Rightarrow 5 + L_f = 50 \frac{m_2}{m_1}$$

$$\Rightarrow L_f = \frac{50m_2}{m_1} - 5$$

#1613056

Topic: Moment of Inertia of Common Bodies

Mass per unit area of a disc of inner radius 'a' and outer radius 'b' is given by $\left(\frac{\sigma_0}{r}\right)$, r distance from center. Its radius of gyration w.r.t. axis of rotation passing through center and

perpendicular to plane is

- A $\sqrt{\frac{b^4 - a^4}{3(b^2 - a^2)}}$
 B $\sqrt{\frac{b^3 - a^3}{3(b - a)}}$
 C $\sqrt{\frac{b^3 - a^3}{5(b - a)}}$

$$D \quad \sqrt{\frac{b^4 - a^4}{5(b^2 - a^2)}}$$

Solution

$$I = \int dm \cdot r^2$$

$$I = \int_a^b \frac{\sigma_0}{r} 2\pi r dr \cdot r^2$$

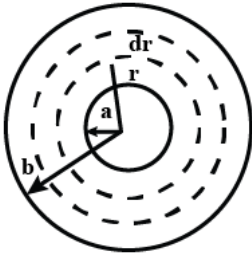
$$I = \sigma_0 2\pi \left(\frac{b^3 - a^3}{3} \right)$$

$$M = \int_a^b dm = b \left[\frac{\sigma_0}{r} 2\pi r dr \right] = \sigma_0 2\pi (b - a)$$

$$I = MK^2$$

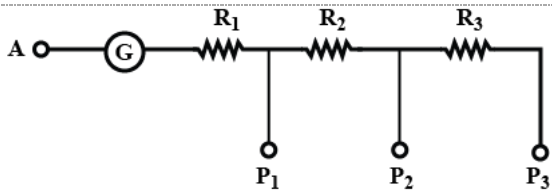
$$\sigma_0 2\pi \left(\frac{b^3 - a^3}{3} \right) = \sigma_0 2\pi (b - a) K^2$$

$$K = \sqrt{\frac{b^3 - a^3}{3(b - a)}}$$



#1613100

Topic: Resistance and Resistivity



A galvanometer has 50 division, current per unit deflection is $20 \mu A$ and resistance of coil of galvanometer is 100Ω . Find the value of resistance R_1 , R_2 and R_3 if its range as a voltmeter when used between A and P_1 is (0, -2 V) between A and P_2 is (0 - 10 V) and between A and P_3 is (0 - 20 V)

- A 1900 Ω , 800 Ω , 10000 Ω
- B 1900 Ω , 4000 Ω , 8000 Ω
- C 19000 Ω , 8800 Ω , 12000 Ω
- D 12000 Ω , 8800 Ω , 19000 Ω

Solution

$$I_G = 20 \times 50 \mu A = 1 mA$$

$$I_G(100 + R_1) = 2$$

$$R_1 = 1900 \Omega$$

$$I_G(100 + R_1 + R_2) = 10 V$$

$$R_2 = 8000 \Omega$$

$$I_G(100 + R_1 + R_2 + R_3) = 20$$

$$R_3 = 10000 \Omega$$

#1613104

Topic: Basics of Projectile Motion

Two projectiles are thrown with same speed in such a way that their ranges are equal. If the time of flight for the two projectiles are t_1 and t_2 the value of $t_1 t_2$ in terms of range ' R ' and ' g ' is

- A $\frac{R}{g}$
- B** $\frac{2R}{g}$
- C $\frac{R}{2g}$
- D $\frac{R}{4g}$

Solution

$$t_1 = \frac{2u \sin \theta_1}{g}$$

$$t_2 = \frac{2u \sin \theta_2}{g}$$

$$t_1 t_2 = \frac{4u^2}{g^2} \sin \theta_1 \sin \theta_2 \quad \because \text{range are equal}$$

$$\theta_2 = 90^\circ - \theta_1$$

$$\therefore t_1 t_2 \frac{2 \cdot 2u^2 \sin \theta_1 \cos \theta_1}{g} = \frac{2R}{g}$$

#1613113

Topic: Magnetic Moment

A dipole is placed at the origin such that its dipole moment is $p\hat{i}$. The electric field and potential at $(0, d, 0)$ respectively are:

- A $\frac{p}{4p\epsilon_0 d^3} \hat{i}, 0$
- B** $\frac{-p}{4p\epsilon_0 d^3} \hat{i}, 0$
- C $\frac{2p}{4p\epsilon_0 d^3} \hat{i}, 0$
- D $\frac{-2p}{4p\epsilon_0 d^3} \hat{i}, 0$

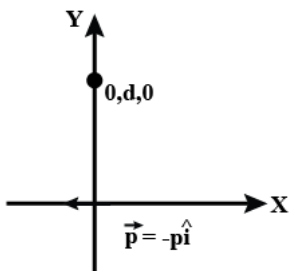
Solution

Clearly it is the axial position

$$\vec{E} = -\frac{k\vec{p}}{r^3} = \frac{1}{4\pi\epsilon_0} \frac{p}{r^3} \hat{i}$$

put $r = d$

$$\vec{E} = -\frac{p}{4\pi\epsilon_0 d^3} \hat{i} \Rightarrow V = 0$$



#1613114

Topic: Musical sound and scale

Submarine A is going with speed of 18km/hr. Submarine B is chasing A with speed of 27 km/hr. It sends frequency of 500Hz and hears after reflection from A. The perceived frequency is:

- A 500Hz
- B** 502Hz
- C 498Hz
- D 504Hz

Solution

By using Doppler effect,

$$\text{Frequency received by A, } f_A = f_0 \left(\frac{1500 - 5}{1500 - 7.5} \right)$$

$$\text{Frequency of reflected sound perceived by B} = f_A \left(\frac{1500 + 7.5}{1500 + 5} \right) = 500 \left(\frac{1500 - 5}{1500 + 7.5} \right) \left(\frac{1500 + 7.5}{1500 + 5} \right) = 501.699 \cong 502 \text{ Hz}$$



#1613121

Topic: Electric Field

The electric field is space given by $\vec{E} = E_0 \sin(\Omega t + 6y - 8z) \hat{n}$ then the direction of propagation of light wave is

- A $\frac{-3\hat{j} - 4\hat{k}}{5}$
- B $\frac{-3\hat{j} + 4\hat{k}}{5}$
- C $\frac{-3\hat{j} - 4\hat{k}}{5}$
- D $\frac{3\hat{j} - 4\hat{k}}{5}$

#1613140

Topic: Resistance and Resistivity

Dimension of resistance R in terms of μ_0 & ϵ_0 are

- A $\sqrt{\frac{\mu_0}{\epsilon_0}}$
- B $\sqrt{\frac{\epsilon_0}{\mu_0}}$
- C $\frac{\epsilon_0}{\mu_0}$
- D $\frac{\mu_0}{\epsilon_0}$

Solution

$$[\mu_0] = [M^1 L^2 T^{-2} A^{-2}]$$

$$[R] = [M L^2 T^{-3} A^{-2}]$$

$$[R] = [\epsilon_0]^a [\mu_0]^b$$

$$[M L^2 T^{-3} A^{-2}] = [M^{-a} L^{-3a} T^{4a} A^{2a} M^b L^{2b} T^{-2b} A^{-2b}]$$

$$2a - 2b = -2$$

$$a - b = -1 \dots (1)$$

$$4a - 2b = -3 \dots (2)$$

$$2a - 2b = -2 \dots (3)$$

$$2a = -1$$

$$a = -\frac{1}{2}, b = \frac{1}{2}$$

$$R \rightarrow [R] = \left[\sqrt{\frac{\mu_0}{\epsilon_0}} \right]$$

#1613143

Topic: Interference

In YDSE when slab of thickness t and refractive index μ is placed in front of one slit then central maxima shifts by one fringe width. Find out t in terms of λ and μ

- A $\frac{\lambda}{(2\mu - 1)}$

B $\frac{2\lambda}{(2\mu - 1)}$

C $\frac{\lambda}{(\mu - 1)}$

D $\frac{2\lambda}{(2\mu + 1)}$

Solution

when a film of thickness t and refractive index μ is introduced in the path of one of the source of light ,then fringe shift occur as optical path difference changes

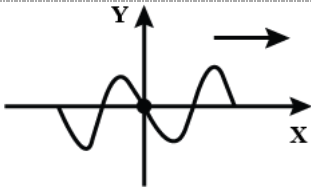
$$\Delta y = (\mu - 1) \frac{tD}{d}$$

And, $\beta = \frac{\lambda D}{d}$

So, $t = \frac{\lambda}{(\mu - 1)}$

#1613153

Topic: Waves on a String



A wave is propagating in positive x - direction . A time $t = 0$ its snapshot is taken as shown .If the wave equation is $y = A\sin(\omega t - kx + \phi)$, then ϕ is

A $\phi = 0$

B $\phi = \pi$

C $\phi = \frac{\pi}{2}$

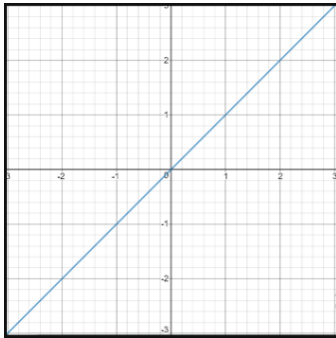
D $\phi = 3\pi/2$

Solution

At $t = 0$, the phase of particle at $x = 0$ is 0

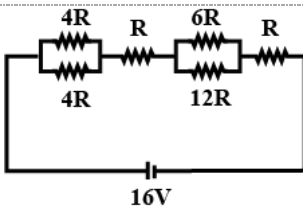
$\therefore \phi = 0$

Thus the graph will be in the straight line passing through the origin.



#1613157

Topic: Resistance and Resistivity



If the power dissipated in the circuits is $4W$ then the value of R is :

A 4Ω

B 8Ω

C 16Ω

D 12Ω

Solution

$$\text{As } P = \frac{V^2}{R},$$

further solving it we get,

$$R_{eq} = \frac{V^2}{P} = \frac{16^2}{4} = 64\Omega$$

$$2R + R + 4R + R = 64$$

$$8R = 64$$

$$R = 8\Omega$$

#1613164

Topic: Basics of Projectile Motion

Equation of trajectory of ground to ground projectile is $y = 2x - 9x^2$. Then the angle of projection with horizontal and speed of projection is: ($g = 10\text{m/s}^2$)

- A $\tan^{-1}(2), \frac{5}{3}\text{m/s}$
- B $\tan^{-1}(3), \frac{5}{3}\text{m/s}$
- C $\tan^{-1}(2), \frac{2}{3}\text{m/s}$
- D $\tan^{-1}(3), \frac{2}{3}\text{m/s}$

Solution

$$y = 2x - 9x^2 \quad \dots\dots\dots\text{Equ 1}$$

$$y = x \tan\theta - \frac{1}{2} \frac{gx^2}{u^2 \cos^2\theta} \quad \dots\dots\dots\text{Equ 2}$$

comparing these two equations we get,

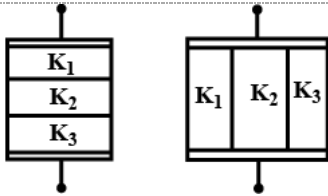
$$\tan\theta = 2$$

$$\frac{g}{2u^2 \cos^2\theta} = 9$$

$$\frac{10(1+4)}{2u^2} = 9 \Rightarrow u^2 = \frac{10 \times 5}{2 \times 9} \Rightarrow u = \frac{5}{3}\text{m/s}$$

#1613172

Topic: Dielectrics in capacitors



Two parallel plate capacitors are filled with dielectrics and connected separately across same potential difference as shown in figure. their plate area is A and separation between plates is 'd'. then the ration of energy stored is:

- A $\frac{9K_1K_2K_3}{(K_1K_2 + K_2K_3 + K_3K_1)(K_1 + K_2 + K_3)}$
- B $\frac{5K_1K_2K_3}{(K_1K_2 + K_2K_3 + K_3K_1)(K_1 + K_2 + K_3)}$
- C $\frac{6K_1K_2K_3}{(K_1K_2 + K_2 + K_3 + K_3 + K_1)(K_1 + K_2 + K_3)}$
- D $\frac{3K_1K_2K_3}{(K_1K_2 + K_2K_3 + K_3K_1)(K_1 + K_2 + K_3)}$

Solution

$$\frac{1}{C_1} = \frac{d}{K_1 \epsilon_0 A} + \frac{d}{K_2 \epsilon_0 A} + \frac{d}{K_3 \epsilon_0 A} \text{ s}$$

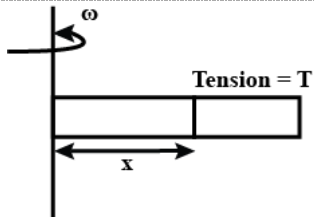
$$C_1 = \frac{3K_1 K_2 K_3 \epsilon_0 A}{d(K_1 K_2 + K_2 K_3 + K_3 K_1)}$$

$$C_2 = \frac{(K_1 + K_2 + K_3) \epsilon_0 A}{3d}$$

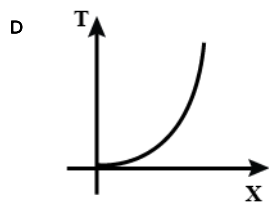
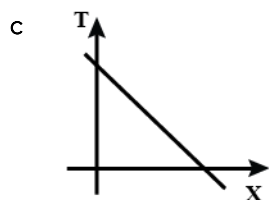
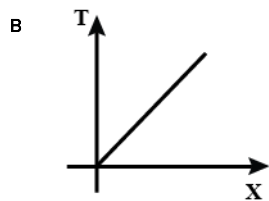
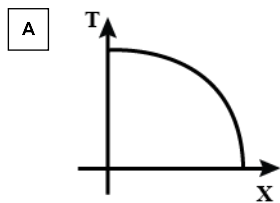
$$\frac{E_1}{E_2} = \frac{\frac{1}{2} C_1 V^2}{C_2 V^2} = \frac{9K_1 K_2 K_3}{(K_1 K_2 + K_2 K_3 + K_3 K_1)(K_1 + K_2 + K_3)}$$

#1613179

Topic: Torque



A uniform rod of length l is rotating with constant angular speed ω as shown in figure. Choose the graph which correctly shows the variation of T with x



Solution

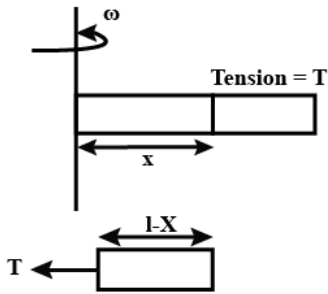
By using the concept of Rotational motion on body ,

tension can be given as:

$$T = \frac{m}{l}(l-x)\omega^2 \left(x + \frac{l-x}{2} \right)$$

$$T = \frac{m}{l}(\omega^2) \frac{(l-x)(l+x)}{2}$$

$$T = \frac{m\omega^2}{2l} (l^2 - x^2)$$



#1613184

Topic: Elastic Collisions in One-Dimension



Two men A and B of mass 50kg and 20kg respectively are at rest on a frictionless surface as shown in figure. If A pushes B with relative velocity 0.7 m/s then find velocity of A just after the push

- A 0.2m/s
- B 1m/s
- C 5m/s
- D 4m/s

Solution

$$P_i = 0$$

$$P_f = 20(0.7 - v) - 50(v)$$

$$20(0.7 - v) = 50v$$

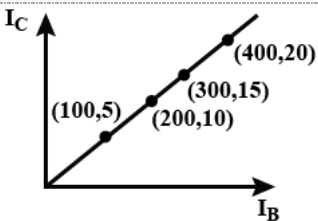
$$14 - 20v = 50v$$

$$14 = 70v$$

$$v = \frac{14}{70} = 0.2m/s$$

#1613192

Topic: Basics of AC



Graph between output current (I_c) and input current (I_b) for common emitter of $n-p-n$ transistor is given in the figure. If input resistance is $100k\Omega$. Find the out voltage gain and power gain are

- A $2 \times 10^4, 4 \times 10^5$
- B $3 \times 10^4, 9 \times 10^6$
- C $6 \times 10^4, 8 \times 10^6$

D $8 \times 10^4, 2 \times 10^6$

Solution

$$\text{Current gain } (\beta) = \frac{\Delta I_C}{\Delta I_B} = \left(\frac{200 - 100}{10 - 5} \right) = \frac{100}{5} = 20$$

$$\text{Voltage gain } (A_V) = \beta \times \frac{R_{out}}{R_{in}} = 20 \times \frac{100 \times 10^3}{100} = 20 \times 10^3$$

$$\text{Power gain} = A_V \times \beta = 20 \times 10^3 \times 20 = 4 \times 10^5$$

#1613196

Topic: Magnetic field

A point charge is moving in a circular path of radius 10cm with angular frequency $40\pi\text{ rad/s}$. The magnetic field produced by it at the center is $3.8 \times 10^{-10}\text{ T}$. Then the value of charge is :

- A $3\mu\text{C}$
- B $4\mu\text{C}$
- C $1\mu\text{C}$
- D $9\mu\text{C}$

Solution

$$B = \frac{\mu_0 qv}{4\pi r^2} \sin\theta$$

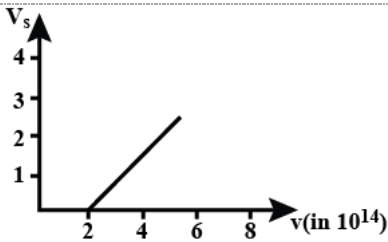
$$B = 10^{-7} \frac{q\omega r}{r^2}$$

$$= 3.8 \times 10^{-10} = 10^{-7} \cdot q \times 40\pi$$

$$q = 3\mu\text{C}$$

#1613205

Topic: Stopping Potential and Einstein's Photoelectric Equation



Graph between stopping potential and frequency of photon is given in figure.

Find out work function metal

- A 0.82
- B 0.92
- C 0.72
- D 0.62

Solution

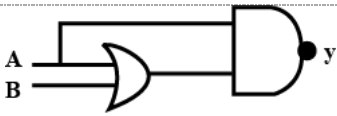
$$v_{th} = 2 \times 10^{14}\text{ Hz}$$

$$W = \frac{h\nu_{th}}{e} \text{ (in eV)}$$

$$W = \frac{6.63 \times 10^{-34} \times 2 \times 10^{14}}{1.6 \times 10^{19}} = 0.82\text{ eV}$$

#1613210

Topic: Logic Gates



Logic gate for input A and B is given in figure .

Which table is correct for given gates system:

A

A	B	Y
0	0	0
1	0	1
0	1	0
1	1	1

B

A	B	Y
0	0	0
1	0	1
0	1	1
1	1	0

C

A	B	Y
0	0	1
1	0	0
0	1	1
1	1	0

D

A	B	Y
0	0	1
1	0	1
0	1	0
1	1	0

Solution

Output of OR gate $C = A + B$

$y = (A + B) \cdot A$

#1613211

Topic: Diffraction

If aperture diameter of the lens of a telescope is 1.25 m and wavelength of light used is 5000 \AA its resolving power is

- A 2.05×10^6
- B 2.5×10^5
- C 4.1×10^5
- D 4.1×10^6

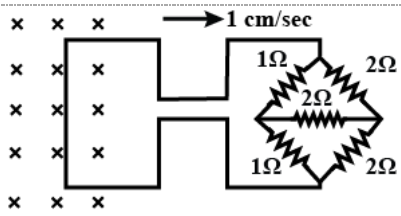
Solution

$$\text{resolving power} = \frac{d}{1.22\lambda} = \frac{1.25 \times 10^{10}}{1.22 \times 500}$$

$$\Rightarrow 2.049 \times 10^6$$

#1613212

Topic: Magnets



A square wire of resistance 1.3Ω and side 1cm its moving in uniform magnetic field $B = 1\text{T}$ with speed $1\text{cm}/\text{sec}$ as shown in figure the the currnet in loops is:

- A $41\mu A$
- B $54\mu A$
- C $61\mu A$
- D $31\mu A$

Solution

$$E = Bv = 1 \times 10^{-2} \times 10^{-2} = 10^{-4} \text{ Volt}$$

$$R_{eq} = \frac{4}{3} + 1.3 = 1.33 + 1.3 = 1.63\Omega$$

$$I = \frac{10^{-4}}{1.63} = 61\mu A$$